$\qquad$
$\qquad$ Date: $\qquad$

## Polar Coordinates Word Problems

A surveyor mapping out the land where a new housing development will be built identifies a landmark 223 feet away and $45^{\circ}$ left of center. A second landmark is 418 feet away and $70^{\circ}$ right of center.

1. Sketch a graph to find the actual angles made by the points.
2. Find the distance between two points.
$\qquad$ Period: $\qquad$ Date: $\qquad$

## Polar Coordinates Word Problems

## Answers

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1. Sketch a graph to find the actual angles made by the points.


For $\boldsymbol{P}_{1}$, angle $\boldsymbol{\theta}_{\mathbf{1}}$ is $\mathbf{9 0}^{\circ}-\mathbf{7 0}^{\circ}=\mathbf{2 0 ^ { \circ }}$ and $r_{1}=418$
For $P_{2}$, angle $\theta_{2}$ is $90^{\circ}+45^{\circ}=135^{\circ}$ and $r_{2}=223$
$\rightarrow P_{1}\left(418,20^{\circ}\right)$ and $P_{2}\left(223,135^{\circ}\right)$
2. Find the distance between two points.

The distance formula is,

$$
\begin{aligned}
& P_{1} P_{2}=\sqrt{r_{1}^{2}+r_{2}^{2}-2 r_{1} r_{2} \cos \left(\theta_{2}-\theta_{1}\right)} \\
& P_{1} P_{2}=\sqrt{418^{2}+223^{2}-2(418)(223) \cos \left(135^{\circ}-20^{\circ}\right)} \\
& P_{1} P_{2}=\sqrt{224453-186428 \cos \left(115^{\circ}\right)} \\
& \rightarrow P_{1} P_{2}=550
\end{aligned}
$$

