Ellipses and Circles Bell Work

Write each equation in standard form and identify the conic related to it.

1. $x^2 + y^2 + 6x - 4y - 3 = 0$

2. $3x^2 + y^2 + 42x + 4y + 142 = 0$

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Answers

Write each equation in standard form and identify the conic related to it.

1. $x^2 + y^2 + 6x - 4y - 3 = 0$

 $x^{2} + 6x + 9 + y^{2} - 4y + 4 - 3 = 0 + 9 + 4$

$$(x+3)^2 + (y-2)^2 = 13+3$$

$$(x+3)^2 + (y-2)^2 = 16$$

Because a = b, and the equation is of the form $(x - h)^2 + (y - k)^2 = r^2$

 \rightarrow The conic is a circle.

2.
$$3x^2 + y^2 + 42x + 4y + 142 = 0$$

$$3x^{2} + 42x + 147 + y^{2} + 4y + 4 + 142 = 0 + 147 + 4$$

$$3(x^{2} + 14x + 49) + (y^{2} + 4y + 4) + 142 = 151$$

$$3(x + 7)^{2} + (y + 2)^{2} = 9$$

$$\frac{(x + 7)^{2}}{3} + \frac{(y + 2)^{2}}{9} = 1$$

Because $a \neq b$, and the equation is of the form $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$

 \rightarrow The conic is an ellipse.