**Increasing and Decreasing Behavior**

A function is increasing on an interval if and only if for every and contained in , , whenever .

A function is decreasing on an interval if and only if for every and contained in , whenever .

A function remains constant on an interval if and only if for every and contained in , whenever .

Points in the domain of a function where the function changes from increasing to decreasing or from decreasing to increasing are called **critical points.** At these points, a line drawn tangent to the curve is horizontal or vertical.

**Sample Problem 1: Use the graph of each function to estimate intervals on which the function is increasing, decreasing, or constant. Support the answer numerically.**

|  |  |  |
| --- | --- | --- |
| **a.** |  |  |
| **b.** |  |  |

**Extrema** are critical points at which a function changes its increasing or decreasing behavior. At these points, the function has a maximum or a minimum value, either relative or absolute.

The greatest value that a function assumes over its domain is called the **absolute maximum**.

The least value that a function assumes over its domain is called the **absolute minimum**.

**A relative maximum value** of a function may not be the greatest value of on the domain, but it is the greatest value on some interval of the domain.

**A relative minimum** **value** of a function is the least value on some interval of the domain.

**A point of inflection** can also be a critical point. At these points, the graph changes its shape, but not it’s increasing or decreasing behavior. Instead, the curve changes from being bent upward to being bent downward, or vice versa.

**Sample Problem 2**: **Estimate and classify the extrema for the graph of each function. Support the answers numerically.**

|  |  |  |
| --- | --- | --- |
| **a.** |  |  |
| **b.** |  |  |

**Average Rate of Change**

The average rate of change between any two points on the graph of is the slope of the line through those points.

The line through two points on a curve is called a secant line. The slope of the secant line is denoted **.**

The average rate of change on the interval is:

When the average rate of change over an interval is positive, the function increases on average over that interval.

When the average rate of change is negative, the function decreases on average over that interval.

**Sample Problem 3:**  **Find the average rate of change of each function on the given interval.**

|  |  |  |  |
| --- | --- | --- | --- |
| **a.** |  | **b.** |  |
|  |  |  |  |

**Computing Average Rate of Change from a Graph**

**Sample Problem 4:**  **Find the average rate of change of a function on the given interval.**

|  |  |  |
| --- | --- | --- |
| **a.** |  |  |